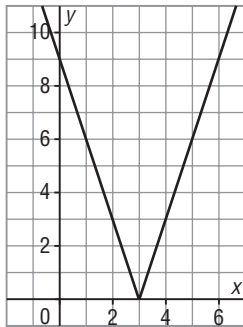


# PRACTICE TEST, pages 698–700

1. **Multiple Choice** Which solution is correct for  $|x^2 - 6x + 5| = 5$ ?

- A. no solution                      B.  $x = 0$   
 C.  $x = 0$ ;  $x = 6$ ;  $x = \frac{1}{3}$ ;  $x = \frac{2}{3}$     **D.**  $x = 0$ ;  $x = 6$

2. **Multiple Choice** Which function describes this graph?



- A.  $y = |3x + 9|$   
**B.**  $y = |3x - 9|$   
 C.  $y = |-\frac{1}{3}x + 9|$   
 D.  $y = |9x + 3|$

3. Solve each equation.

a)  $|-4x + 4| = 2$

$$\begin{aligned} -4x + 4 &= 2 \\ \text{if } -4x + 4 &\geq 0 \\ \text{that is, if } x &\leq 1 \\ \text{When } x \leq 1: \\ -4x + 4 &= 2 \\ -4x &= -2 \\ x &= \frac{1}{2} \end{aligned}$$

$\frac{1}{2} \leq 1$ , so this root  
is a solution.

The solutions are  $x = \frac{1}{2}$  and  $x = \frac{3}{2}$ .

$$\begin{aligned} -(-4x + 4) &= 2 \\ \text{if } -4x + 4 &< 0 \\ \text{that is, if } x &> 1 \\ \text{When } x > 1: \\ -(-4x + 4) &= 2 \\ -4x + 4 &= -2 \\ 4x &= 6 \\ x &= \frac{3}{2} \end{aligned}$$

$\frac{3}{2} > 1$ , so this root  
is a solution.

b)  $x + 1 = |x^2 - 4x + 5|$

$$\begin{aligned} \text{When } x^2 - 4x + 5 &\geq 0: \\ x + 1 &= x^2 - 4x + 5 \\ 0 &= x^2 - 5x + 4 \\ 0 &= (x - 1)(x - 4) \\ x &= 1 \text{ or } x = 4 \end{aligned}$$

So,  $x = 1$  and  $x = 4$  are the solutions.

$$\begin{aligned} \text{When } x^2 - 4x + 5 &< 0: \\ x + 1 &= -(x^2 - 4x + 5) \\ x + 1 &= -x^2 + 4x - 5 \\ x^2 - 3x + 6 &= 0 \\ x &= \frac{3 \pm \sqrt{(-3)^2 - 4(1)(6)}}{2(1)} \\ x &= \frac{3 \pm \sqrt{-15}}{2} \end{aligned}$$

This is not a real number.

4. Sketch a graph of each absolute value function. Identify the intercepts, domain, and range. Write the functions in piecewise notation.

a)  $y = |5x - 4|$

Draw the graph of  $y = 5x - 4$ .

It has  $x$ -intercept  $\frac{4}{5}$ .

Reflect, in the  $x$ -axis, the part of the graph that is below the  $x$ -axis.

The  $x$ -intercept is  $\frac{4}{5}$ , the  $y$ -intercept is 4, the domain of  $y = |5x - 4|$  is  $x \in \mathbb{R}$ , and the range is  $y \geq 0$ .

$y = 5x - 4$  when

$$5x - 4 \geq 0, \text{ or } x \geq \frac{4}{5}$$

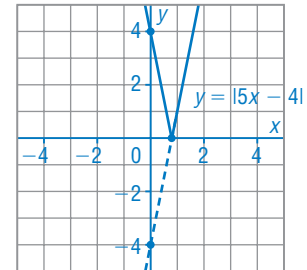
$y = -(5x - 4)$ , or

$y = -5x + 4$  when

$$5x - 4 < 0, \text{ or } x < \frac{4}{5}$$

So, using piecewise notation:

$$y = \begin{cases} 5x - 4, & \text{if } x \geq \frac{4}{5} \\ -5x + 4, & \text{if } x < \frac{4}{5} \end{cases}$$



b)  $y = |-x^2 + 2x + 8|$

The graph of  $y = -x^2 + 2x + 8$ , or  $y = -(x - 4)(x + 2)$  opens down with  $x$ -intercepts 4 and  $-2$ .

Its vertex is on the axis of symmetry,  $x = 1$ , and has coordinates  $(1, 9)$ .

Reflect, in the  $x$ -axis, the part of the graph that is below the  $x$ -axis.

From the graph, the  $x$ -intercepts are  $-2$  and  $4$ , the  $y$ -intercept is  $8$ .

The domain of  $y = |-x^2 + 2x + 8|$  is  $x \in \mathbb{R}$  and the range is  $y \geq 0$ .

The graph of the quadratic function opens down, so between the  $x$ -intercepts, the graph is above the  $x$ -axis.

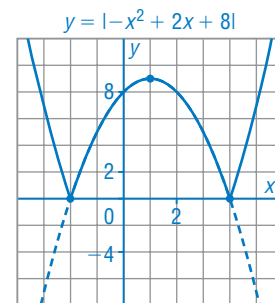
For the graph of  $y = |-x^2 + 2x + 8|$ :

For  $-2 \leq x \leq 4$ , the value of  $-x^2 + 2x + 8 \geq 0$

For  $x < -2$  or  $x > 4$ , the value of  $-x^2 + 2x + 8 < 0$ ; that is,  $y = -(-x^2 + 2x + 8)$ , or  $y = x^2 - 2x - 8$ .

So, using piecewise notation:

$$y = \begin{cases} -x^2 + 2x + 8, & \text{if } -2 \leq x \leq 4 \\ x^2 - 2x - 8, & \text{if } x < -2 \text{ or } x > 4 \end{cases}$$



5. Sketch a graph of the function  $y = \frac{1}{-3x(x-1)}$ .

Label the asymptotes with their equations.

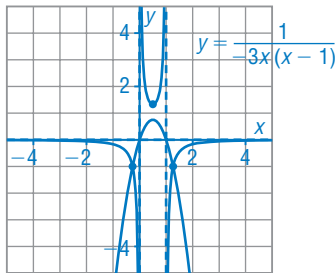
The graph of  $y = -3x(x-1)$  opens down, has  $x$ -intercepts 0 and 1, and vertex  $(0.5, \frac{3}{4})$ . The graph

of  $y = \frac{1}{-3x(x-1)}$  has vertical asymptotes  $x = 0$  and  $x = 1$ , and a horizontal asymptote  $y = 0$ . Plot points where the line  $y = -1$  intersects the graph of  $y = -3x(x-1)$ . These points are common to both graphs.

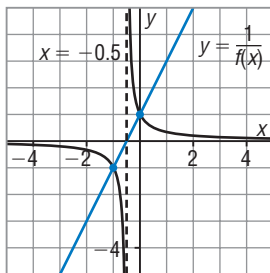
Point  $(0.5, -\frac{3}{4})$  lies on  $y = -3x(x-1)$ ,

so point  $(0.5, \frac{4}{3})$  lies on  $y = \frac{1}{-3x(x-1)}$ .

The graph of the reciprocal function has Shape 3.



6. Use the graph of the reciprocal function  $y = \frac{1}{f(x)}$  to graph the linear function  $y = f(x)$ . Describe your strategy.



Vertical asymptote is  $x = -0.5$ , so graph of  $y = f(x)$  has  $x$ -intercept  $-0.5$ . Mark points at  $y = 1$  and  $y = -1$  on graph of  $y = \frac{1}{f(x)}$ , then draw a line through these points for the graph of  $y = f(x)$ .